

Bottom-Up Parsing

Thanks to Charles E. Hughes

Reductions

- Top-down focuses on producing an input string from the start symbol
- Bottom-up focuses on reducing the string to the start symbol
- By definition, reduction is the reverse of production

Handle Pruning

- Bottom-up reverses a rightmost derivation since rightmost rewrites the leftmost non-terminal last
- Bottom-up must identify a**handle** of a sentential form (a string of terminals and non-terminals derived from the start symbol), where the handle is the substring that was replaced at the last step in a rightmost derivation leading to this sentential form.
- A handle must match the body (rhs) of some production
- Formally, if $S \Rightarrow_{rm}^* \alpha A \omega \Rightarrow_{rm} \alpha \beta \omega$ where $A \rightarrow \beta$ then β , in the position following α , is a handle of $\alpha \beta \omega$
- We would like handles to be unique, and they are so in unambiguous grammars
- Handle pruning is the process of reducing a sentential form to a deriving sentential form by reversing the last production

shift/reduce Parsing

- This involves a stack that holds the left part of a sentential for with the input holding the right part
- Initially the stack has a bottom of stack marker and the input is the entire string to be parsed, plus an end marker Stack = \$ Input = w\$
- Our goal is to consume the string and end up with the start symbol on stack
 Stack = \$\$ Input = \$

shift/reduce Process

- The process is one where we can either
 - Shift the next input symbol onto stack
 - Reduce "handle" on top of stack
 - Accept if successfully get to start symbol with all input consumed
 - Error is a syntax error is discovered

Conflicts in shift/reduce

- Handle pruning can encounter two types of conflicts
 - reduce/reduce is when there are two possible reductions and we cannot decide which to use
 - shift/reduce conflict is when we cannot decided whether to shift or reduce

Classic shift/reduce

$stmt \rightarrow$ if expr then stmt|if expr then stmt else stmt|other

Input = **else** ... \$

Should we shift **else** into stack or reduce??

Can prefer shift over reduce, but that may not work as a general policy

Classic reduce/reduce

If have two types of expression lists preceded by an id. One is array reference using parentheses and other is a function call. Both can appear by themselves. Relevant rules are:

stmt	\rightarrow	id (<i>p_list</i>)
		expr
p_list	\rightarrow	p_list parm parm
e_list	\rightarrow	e_list parm expr
expr	\rightarrow	id(<i>e_list</i>) id
parm	\rightarrow	id
Stack =	= \$id(id	Input = , id)\$

Is this first *expr* or a *parm*?

One solution is that we differentiate **procid** from **id** in symbol table and hence via lexical analysis. Then the third symbol in stack, not part of handle, determines the reduction. The key is context.



Find a useful subset of context free grammars that

- 1.Covers all or at least most unambiguous CF languages
- 2.Is easy to recognize
- 3.Avoids conflicts without severely limiting expressiveness
- 4.Is amenable to a fast parsing algorithm

LR Parsing



- LL(k), k>1, languages ⊃ LL(k-1) languages
 LR(1) languages ⊃ LL(k) languages, k ≥ 0
- LR(k), k>1, languages = LR(1) languages
- However, LR(k), $k \ge 1$, grammars $\supset LR(k-1)$ grammars
- LR grammars can find errors quickly, but they do not always have good context to recover

LR Parser Types

- SLR simple LR parser
- LALR -look-head LR parser
- LR most general LR parser
- SLR, LALR and LR are closely related
 - The parsing algorithm is the same
 - Their parsing tables are different



Configuration of LR Algorithm

• A configuration of a LR parsing is:



- S_m and a_i decide the parser action by consulting the parsing action table. (*Initial Stack* contains just S_o)
- A configuration of a LR parsing represents the right sentential form:

 $X_1 \dots X_m a_i a_{i+1} \dots a_n$ \$

Actions of LR-Parser

 shift s -- shifts the next input symbol onto the stack. Shift is performed only if action[s_m,a_i] = sk, where k is the new state. In this case

 $(S_{o} X_{1} S_{1} ... X_{m} S_{m}, a_{i} a_{i+1} ... a_{n} \$) \twoheadrightarrow (S_{o} X_{1} S_{1} ... X_{m} S_{m} \frac{a_{i} k}{a_{i+1}} ... a_{n} \$)$

- **2.** reduce $A \rightarrow \beta$ (if action[s_m, a_i] = rn where n is a production number)
 - pop $2|\beta|$ items from the stack;
 - then push A and k where k=goto[s_{m-lβl},A]

 $(S_{o} X_{1} S_{1} ... X_{m} S_{m}, a_{i} a_{i+1} ... a_{n} \$) \rightarrow (S_{o} X_{1} S_{1} ... X_{m-|\beta|} S_{m-|\beta|} A k, a_{i} ... a_{n} \$)$

- Output is the reducing production reduce $A \rightarrow \beta$ or the associated semantic action or both
- **3.** Accept Parsing successfully completed
- 4. Error -- Parser detected an error (empty entry in action table)

Reduce Action

- pop 2| β | (=j) items from the stack; let us assume that $\beta = Y_1 Y_2 \dots Y_j$
- then push A and s where s=goto[s_{m-j},A]

$$(S_{o} X_{1} S_{1} ... X_{m-j} S_{m-j} Y_{1} S_{m-j+1} ... Y_{j} S_{m}, a_{i} a_{i+1} ... a_{n} \)$$

$$\Rightarrow (S_{o} X_{1} S_{1} ... X_{m-j} S_{m-j} A s, a_{i} ... a_{n} \)$$

• In fact, $Y_1Y_2...Y_j$ is a handle. $X_1 ... X_{m-j} A a_i ... a_n \$ \Rightarrow X_1 ... X_{m-j} Y_1...Y_j a_i a_{i+1} ... a_n \$$

Expression Grammar

Example: Given the grammar:

$E \rightarrow E + T$	$T \rightarrow T * F$	$F \rightarrow id$
E →T	$T \rightarrow F$	F →(E)

Compute Follow.

Follow E {), +, \$ } T {), *, +, \$ } F {), *, +, \$ }

SLR Parsing Tables

- An LR(0) item of a grammar G is a production of G with a dot at some position of the right side.
- Ex: $A \rightarrow aBb$ LR(0) Items: $A \rightarrow aBb$ $A \rightarrow aBb$ $A \rightarrow aBb$ $A \rightarrow aBb$ $A \rightarrow aBb$
- Sets of LR(0) items will be the states of action and goto tables of the SLR parser.
- A collection of sets of LR(0) items (**the canonical LR(0) collection**) is the basis for constructing SLR parsers.
- Augmented Grammar.

G' is G with a new production rule $S' \rightarrow S$ where S' is the new starting symbol.

The Closure Operation

- If *I* is a set of LR(0) items for a grammar G, then *closure(I)* is the set of LR(0) items constructed from *I* by the two rules:
 - 1. Initially, every LR(0) item in *I* is added to *closure(I)*.
 - 2. If $\mathbf{A} \to \alpha \bullet \mathbf{B}\beta$ is in *closure(I)* and $\mathbf{B} \to \gamma$ is a production rule of G; then $\mathbf{B} \to \bullet \gamma$ will be in the *closure(I)*. We will apply this rule until no more new LR(0) items can be added to *closure(I)*.

Closure Example

 $E' \rightarrow E$ $E \rightarrow E+T$ $E \rightarrow T$ $T \rightarrow T^*F$ $T \rightarrow F$ $F \rightarrow (E)$ $F \rightarrow id$

 $closure(\{E' \rightarrow \mathbf{I}E\}) =$ $\{ E' \rightarrow \mathbf{E}$ kernel item $E \rightarrow E+T$ $E \rightarrow T$ $T \rightarrow T^*F$ $T \rightarrow F$ $F \rightarrow (E)$ $F \rightarrow id \}$

Closure Algorithm

```
function closure ( I )
begin
J := I;
```

repeat

for each item $A \rightarrow \alpha . B\beta$ in J and each production $B \rightarrow \gamma$ of G such that $B \rightarrow .\gamma$ is not in J do add $B \rightarrow .\gamma$ to J; until no more items can be added to J; return J;

end

Goto Function

If I is a set of LR(0) items and X is a grammar symbol (terminal or non-terminal), then goto(I,X) is defined as follows:

If $A \rightarrow \alpha \equiv X\beta$ in I then every item in **closure({A \rightarrow \alpha X \equiv \beta})** will be in goto(I,X).

If I is the set of items that are valid for some viable prefix γ , then goto(I,X) is the set of items that are valid for the viable prefix γX .

Example:

```
\begin{split} \mathsf{I} = \{ & \mathsf{E}' \to \bullet \mathsf{E}, \ \mathsf{E} \to \bullet \mathsf{E} + \mathsf{T}, \ \mathsf{E} \to \bullet \mathsf{T}, \\ & \mathsf{T} \to \bullet \mathsf{T}^*\mathsf{F}, \ \mathsf{T} \to \bullet \mathsf{F}, \ \mathsf{F} \to \bullet (\mathsf{E}), \ \mathsf{F} \to \bullet \mathsf{id} \ \} \\ goto(\mathsf{I},\mathsf{E}) = \{ & \mathsf{E}' \to \mathsf{E} \bullet, \ \mathsf{E} \to \mathsf{E} \bullet + \mathsf{T} \ \} \\ goto(\mathsf{I},\mathsf{T}) = \{ & \mathsf{E} \to \mathsf{T} \bullet, \ \mathsf{T} \to \mathsf{T} \bullet ^*\mathsf{F} \ \} \\ goto(\mathsf{I},\mathsf{F}) = \{ \mathsf{T} \to \mathsf{F} \bullet \ \} \\ goto(\mathsf{I},\mathsf{F}) = \{ \mathsf{T} \to \mathsf{F} \bullet \ \} \\ goto(\mathsf{I},\mathsf{()}) = \{ \ \mathsf{F} \to (\bullet \mathsf{E}), \ \mathsf{E} \to \bullet \mathsf{E} + \mathsf{T}, \ \mathsf{E} \to \bullet \mathsf{T}, \ \mathsf{T} \to \bullet \mathsf{T}^*\mathsf{F}, \ \mathsf{T} \to \bullet \mathsf{F}, \\ & \mathsf{F} \to \bullet (\mathsf{E}), \ \mathsf{F} \to \bullet \mathsf{id} \ \} \\ goto(\mathsf{I},\mathsf{id}) = \{ \ \mathsf{F} \to \mathsf{id} \bullet \ \} \end{split}
```

Canonical LR(0) Collection

 To create the SLR parsing tables for a grammar G, we will create the canonical LR(0) collection of the grammar G'.

• Algorithm:

 $\boldsymbol{C} \text{ is } \{ \text{ closure}(\{S' \rightarrow \blacksquare S\}) \}$

repeat the followings until no more set of LR(0) items can be added to **C**.

for each I in C and each grammar symbol X

if goto(I,X) is not empty and not in C

add goto(I,X) to \boldsymbol{C}

• The goto function is a deterministic FSA (finite state automaton), DFA, on the sets in C.

Canonical LR(0) Example

$I_0: E' \rightarrow .E$	$I_1: E' \rightarrow E.$	$I_6: E \rightarrow E+.T$	I_9 : E \rightarrow E+T.
$E \rightarrow .E+T$	$E \rightarrow E.+T$	$T \rightarrow .T^*F$	$T \rightarrow T.*F$
E ightarrow .T		$T \rightarrow .F$	
$T \rightarrow .T^*F$	$I_2: E \rightarrow T.$	$F \rightarrow .(E)$	$I_{10}: T \rightarrow T^*F.$
T ightarrow .F	$T \rightarrow T.*F$	$F \rightarrow .id$	
F ightarrow .(E)			
F ightarrow .id	I_3 : T \rightarrow F.	$I_7: T \rightarrow T^*.F$	I_{11} : $F \rightarrow (E)$.
		$F \rightarrow .(E)$	
	$I_4: F \rightarrow (.E)$	$F \rightarrow .id$	
	$E \rightarrow .E+T$		
	E ightarrow .T	$I_8: F \rightarrow (E.)$	
	$T \rightarrow .T^*F$	$E \rightarrow E.+T$	
	T ightarrow .F		
	F ightarrow .(E)		
	F ightarrow .id		
	I_5 : F \rightarrow id.		

DFA of Goto Function



Compute SLR Parsing Table

- 1. Construct the canonical collection of sets of LR(0) items for G'. $C \leftarrow \{I_0, ..., I_n\}$
- 2. Create the parsing action table as follows
 - If a is a terminal, $\mathbf{A} \rightarrow \alpha . \mathbf{a}\beta$ in \mathbf{I}_i and goto(\mathbf{I}_i, \mathbf{a})= \mathbf{I}_j then action[i,a] is **shift j**.
 - If A→α. is in I_i, then action[i,a] is *reduce* A→α for all a in FOLLOW(A) where A≠S'.
 - If $S' \rightarrow S$. is in I_i , then action[i,\$] is *accept*.
 - If any conflicting actions generated by these rules, the grammar is not SLR(1).
- 3. Create the parsing goto table
 - for all non-terminals A, if $goto(I_i, A)=I_j$ then goto[i, A]=j
- 4. All entries not defined by (2) and (3) are errors.
- 5. Initial state of the parser contains $S' \rightarrow .S$

(SLR) Parsing Tables												
Action Table Goto Table												
0)	$E' \rightarrow E$	state	id	+	*	()	\$		E	Τ	F
1)	$E \rightarrow E+T$	0	s5			s4				1	2	3
・) つ)		1		s6				acc				
Z)	$\Box \rightarrow I$	2		r2	s7		r2	r2				
3)	$T \rightarrow T^*F$	3		r4	r4		r4	r4				
4)	$T \rightarrow F$	4	s5			s4				8	2	3
5)	$F \rightarrow (E)$	5		r6	rб		r6	rб				
6)	$F \rightarrow id$	6	s5			s4					9	3
0)		7	s5			s4						10
		8		s6			s11					
		9		r1	s7		r1	r1				
		10		r3	r3		r3	r3				
		11		r5	r5		r5	r5				

Actions of SLR-Parser

<u>stack</u>	<u>input</u>	action	<u>output</u>
0	id*id+id\$	shift 5	
0id5	*id+id\$	reduce by F→id	F→id
0F3	*id+id\$	reduce by T→F	T→F
0T2	*id+id\$	shift 7	
0T2*7	id+id\$	shift 5	
0T2*7id5	+id\$	reduce by F→id	F→id
0T2*7F10	+id\$	reduce by $T \rightarrow T^*F$	T→T*F
0T2	+id\$	reduce by E→T	E→T
0E1	+id\$	shift 6	
0E1+6	id\$	shift 5	
0E1+6id5	\$	reduce by F→id	F→id
0E1+6F3	\$	reduce by T→F	T→F
0E1+6T9	\$	reduce by $E \rightarrow E + T$	E→E+T
0E1	\$	accept	

SLR(1) Grammar

- An LR parser using SLR(1) parsing tables for a grammar G is called the SLR(1) parser for G.
- If a grammar G has an SLR(1) parsing table, it is called an SLR(1) grammar.
- Every SLR grammar is unambiguous, but every unambiguous grammar is not an SLR grammar.



- If a state does not know whether it will make a shift operation or reduction for a terminal, we say that there is a shift/reduce conflict.
- If a state does not know whether it will make a reduction operation using the production rule i or j for a terminal, we say that there is a reduce/reduce conflict.
- If the SLR parsing table of a grammar G has a conflict, we say that that grammar is not SLR grammar.

Conflict Example 1



Conflict Example2



SLR Weakness

- In SLR method, state i makes a reduction by A→α when the current token is a:
 if A→α. is in I_i and a is in FOLLOW(A)
- In some situations, βA cannot be followed by the terminal a in a right-sentential form when βα and the state i are on the stack top. This means that making reduction in this case is not correct.



- To avoid some invalid reductions, the states need to carry more information.
- Extra information is put into a state by including a terminal symbol as a second component in an item.
- A LR(1) item is:

 $A \rightarrow \alpha \, \beta, a$

where **a** is the look-head of the LR(1) item

(a is a terminal or end-marker.)

- Such an object is called an LR(1) item.
 - 1 refers to the length of the second component
 - The lookahead has no effect on an item of the form [A $\rightarrow \alpha.\beta,a$], where β is not empty.
 - But an item of the form [A $\rightarrow \alpha$.,a] calls for a reduction by A $\rightarrow \alpha$ only if the next input symbol is a.
 - The set of such a's will be a subset of FOLLOW(A), and could be proper.

LR(1) Item (cont.)

• A state will contain $A \rightarrow \alpha_{\bullet}, a_1$ where $\{a_1, ..., a_n\} \subseteq FOLLOW(A)$

. . .

 $A \rightarrow \alpha_{\bullet}, a_n$

 When β is empty (A → α.,a₁/a₂/../a_n), we do the reduction by A→α only if the next input symbol is in the set {a₁,a₂, ...,a_n} (not for any terminal in FOLLOW(A) as with SLR).

Canonical Collection

- The construction of the canonical collection of the sets of LR(1) items are similar to the construction of the canonical collection of the sets of LR(0) items, except that *closure* and *goto* operations work a little bit different.
- **closure(I)** is: (where I is a set of LR(1) items)
 - every LR(1) item in I is in closure(I)
 - if $A \rightarrow \alpha \cdot B\beta$, a in closure(I) and $B \rightarrow \gamma$ is a rule of G; then $B \rightarrow \cdot \gamma$, b will be in the closure(I) for each terminal b in FIRST(β a).

goto operation

 If I is a set of LR(1) items and X is a grammar symbol (terminal or non-terminal), then goto(I,X) is defined as follows:

- If $A \rightarrow \alpha . X\beta$, a is in I then every item in **closure({A** $\rightarrow \alpha X.\beta,a$ }) will be in goto(I,X).

Canonical LR(1) Collection

• Algorithm:

 $\boldsymbol{C} \text{ is } \{ \text{ closure}(\{\text{S}' \rightarrow . \text{S}, \$\}) \}$

repeat the followings until no more set of LR(1) items can be added to **C**.

for each I in C and each grammar symbol X
if goto(I,X) is not empty and not in C
add goto(I,X) to C

goto function is a DFA on the sets in C.

Short Notation

 A set of LR(1) items containing the following items

 $A \rightarrow \alpha$. β , a_1

 $A \rightarrow \alpha$. β , a_n

can be written as

 $A \rightarrow \alpha \beta_{1}a_{2}/.../a_{n}$

Canonical LR(1) Collection



$$I_4: S \to Aa.Ab , \$ \xrightarrow{A} I_6: S \to AaA.b , \$ \xrightarrow{b} I_8: S \to AaAb. , \$ \xrightarrow{A} A \to . , b$$

I₅: S → Bb.Ba , $\$ \xrightarrow{B}$ I₇: S → BbB.a , $\$ \xrightarrow{a}$ I₉: S → BbBa. , $\$ \xrightarrow{B}$ B → . , a

An Example

 $I_0: closure(\{(S' \rightarrow \bullet S, \$)\}) = (S' \rightarrow \bullet S, \$) \\ (S \rightarrow \bullet C C, \$) \\ (C \rightarrow \bullet c C, c/d) \\ (C \rightarrow \bullet d, c/d)$

 $I_1: goto(I_0, S) = (S' \rightarrow S \bullet, \$)$ $I_2: goto(I_0, C) = (S \rightarrow C \bullet C, \$)$ $(C \rightarrow \bullet c C, \$)$ $(C \rightarrow \bullet d, \$)$

 $I_4: goto(I_0, d) = (C \rightarrow d \bullet, c/d)$

 $I_{5}: goto(I_{2}, C) = (S \rightarrow C C \bullet, \$)$

 $I_{6}: goto(I_{2}, c) = (C \rightarrow c \bullet C, \$)$ $(C \rightarrow \bullet c C, \$)$ $(C \rightarrow \bullet c C, \$)$ $(C \rightarrow \bullet d, \$)$ $: goto(I_{6}, c) = I_{6}$ $: goto(I_{6}, d) = I_{7}$ $1. S' \rightarrow S$ $2. S \rightarrow C C$ $3. C \rightarrow c C$ $4. C \rightarrow d$

 $I_7: goto(I_2, d) = (C \rightarrow d \bullet, \$)$

- $I_8: goto(I_3, C) = (C \rightarrow c C \bullet, c/d)$
- $I_9: goto(I_6, C) = (C \rightarrow c C \bullet, \$)$

 $I_3: goto(I_0, c) = (C \rightarrow c \bullet C, c/d)$ $(C \rightarrow \bullet c C, c/d)$ $(C \rightarrow \bullet d, c/d)$ $: goto(I_3, c) = I_3$ $: goto(I_3, d) = I_4$





An Example

	С	d	\$	S	С
0	s3	s4		1	2
1			а		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

The Core of LR(1) Items

- The core of a set of LR(1) Items is the set of their first components (i.e., LR(0) items)
- The core of the set of LR(1) items $\{ (C \rightarrow c \bullet C, c/d), \\
 (C \rightarrow \bullet c C, c/d), \\
 (C \rightarrow \bullet d, c/d) \}$ is $\{ C \rightarrow c \bullet C, \\
 C \rightarrow \bullet c C, \\
 C \rightarrow \bullet d \}$

Construction of LR(1) Parsing Tables

- 1. Construct the canonical collection of sets of LR(1) items for G'. $C \leftarrow \{I_0, ..., I_n\}$
- 2. Create the parsing action table as follows
 - If **a** is a terminal, **A**→α **a**β,**b** in I_i and goto(I_i,**a**)=I_j then action[i,**a**] is shift j.
 - If $A \rightarrow \alpha$., *a* is in I_i , then action[i, *a*] is *reduce* $A \rightarrow \alpha$ where $A \neq S'$.
 - If $S' \rightarrow S.,$ \$ is in I_i , then action[i, \$] is *accept*.
 - If any conflicting actions are generated by these rules, the grammar is not LR(1).
- 3. Create the parsing goto table
 - for all non-terminals \mathbf{A} , if goto(\mathbf{I}_i, \mathbf{A})= \mathbf{I}_j then goto[i, \mathbf{A}]=j
- 4. All entries not defined by (2) and (3) are errors.
- 5. Initial state of the parser contains $S' \rightarrow .S,$

LALR Parsing Tables

- 1. LALR stands for Lookahead LR.
- 2. LALR parsers are often used in practice because LALR parsing tables are smaller than LR(1) parsing tables.
- 3. The number of states in SLR and LALR parsing tables for a grammar G are equal.
- 4. But LALR parsers recognize more grammars than SLR parsers.
- 5. Bison creates a LALR parser for the given grammar.
- 6. A state of an LALR parser will again be a set of LR(1) items.

Creating LALR Parsing Tables

Canonical LR(1) Parser

LALR Parser

shrink # of states

- This shrink process may introduce a reduce/reduce conflict in the resulting LALR parser (so the grammar is NOT LALR)
- But, this shrink process does not produce a **shift/reduce** conflict.

The Core of Set of LR(1) Items

• The core of a set of LR(1) items is the set of its first component.

Ex: $S \rightarrow L_{\bullet} = R, \$ \rightarrow S \rightarrow L_{\bullet} = R \leftarrow Core$ $R \rightarrow L_{\bullet}, \$ \qquad R \rightarrow L_{\bullet}$

• We will find the states (sets of LR(1) items) in a canonical LR(1) parser with same cores. Then we will merge them as a single state.

$$I_1:L \rightarrow id \bullet ,= \qquad \qquad A \text{ new state:} \qquad I_{12}: L \rightarrow id \bullet ,= \\ \bullet \qquad \qquad \qquad L \rightarrow id \bullet ,\$$$

 $I_2: L \rightarrow id \bullet$, \$ have same core, merge them

- We will do this for all states of a canonical LR(1) parser to get the states of the LALR parser.
- In fact, the number of the states of the LALR parser for a grammar will be equal to the number of states of the SLR parser for that grammar.

Creation of LALR Parsing Tables

- 1. Create the canonical LR(1) collection of the sets of LR(1) items for the given grammar.
- 2. For each core present; find all sets having that same core; replace those sets having same cores with a single set which is their union. $C = \{I_0, ..., I_n\} \rightarrow C' = \{J_0, ..., J_m\}$ where $m \le n$
- 3. Create the parsing tables (action and goto tables) same as the construction of the parsing tables of LR(1) parser.
 - 1. Note that: If $J=I_{i1}\cup ... \cup I_{ik}$ since $I_{i1},...,I_{ik}$ have same cores
 - \rightarrow cores of goto(I_{i1},X),...,goto(I_{ik},X) must be same.
 - So, goto(J,X)=K where K is the union of all sets of items having same cores as goto(I_{i1},X).
- 4. If no conflict is introduced, the grammar is LALR(1) grammar. (We may only introduce reduce/reduce conflicts; we cannot introduce a shift/reduce conflict)









LALR Parse Table



Shift/Reduce Conflict

- We said that we cannot introduce a shift/reduce conflict during the shrink process for the creation of the states of a LALR parser.
- Assume that we can introduce a shift/reduce conflict. In this case, a state of LALR parser must have:

 $A \rightarrow \alpha$, a and $B \rightarrow \beta$ ay, b

• This means that a state of the canonical LR(1) parser must have:

 $A \rightarrow \alpha$, a and $B \rightarrow \beta$ ay, c

But, this state also has a shift/reduce conflict; i.e., the original canonical LR(1) parser has a conflict.

(Reason for this, the shift operation does not depend on lookaheads)

Reduce/Reduce Conflict

• But, we may introduce a reduce/reduce conflict during the shrink process for the creation of the states of a LALR parser.

Canonical LALR(1)– Ex2



$$\begin{split} I_{6}:S \rightarrow L = \bullet R, \$ & \text{to } I_{9} & I_{9}:S \rightarrow L = R \bullet, \$ & \text{Same Cores} \\ R \rightarrow \bullet L, \$ & \text{to } I_{810} & I_{4} \text{ and } I_{11} \\ L \rightarrow \bullet \ast R, \$ & \text{to } I_{411} & I_{5} \text{ and } I_{12} \\ I \rightarrow \bullet \text{id}, \$ & \text{to } I_{512} & I_{7} \text{ and } I_{13} \end{split}$$

 I_8 and I_{10}

 I_{810} : $R \rightarrow L \bullet , $/=$

LALR(1) Parsing- (for Ex2)

	id	*	=	\$	S	L	R
0	s5	s4			1	2	3
1				acc			
2			s6	r5			
3				r2			
4	s5	s4				8	7
5			r4	r4			
6	s12	s11				10	9
7			r3	r3			
8			r5	r5			
9				r1			

no shift/reduce or no reduce/reduce conflict so, it is a LALR(1) grammar

Using Ambiguous Grammars

- All grammars used in the construction of LR-parsing tables must be unambiguous.
- Can we create LR-parsing tables for ambiguous grammars?
 - Yes, but they will have conflicts.
 - We can resolve these conflicts in favor of one of them to disambiguate the grammar.
 - At the end, we will have again an unambiguous grammar.
- Why use an ambiguous grammar?
 - Some of the ambiguous grammars are **more natural**, and a corresponding unambiguous grammar can be very complex.
 - Usage of an ambiguous grammar may eliminate unnecessary reductions.
- Ex.

$$E \rightarrow E+E \mid E^*E \mid (E) \mid id$$

→

 $E \rightarrow E+T | T$ $T \rightarrow T^*F | F$ $F \rightarrow (E) | id$



SLR Tables for Amb Grammar

 $FOLLOW(E) = \{ \$, +, *, \}$

State I_7 has shift/reduce conflicts for symbols + and *.

 $I_0 \xrightarrow{E} I_1 \xrightarrow{+} I_4 \xrightarrow{E} I_7$

when current token is + shift \rightarrow + is right-associative reduce \rightarrow + is left-associative

when current token is *

shift \rightarrow * has higher precedence than + reduce \rightarrow + has higher precedence than *

SLR Tables for Amb Grammar

FOLLOW(E) = { $\$, +, *,) }$

State I_8 has shift/reduce conflicts for symbols + and *.

 $I_{0} \xrightarrow{E} I_{1} \xrightarrow{*} I_{5} \xrightarrow{E} I_{8}$ when current token is *
shift \rightarrow * is right-associative
reduce \rightarrow * is left-associative

when current token is +

shift \rightarrow + has higher precedence than * reduce \rightarrow * has higher precedence than +

SLR Tables for Amb Grammar Action Goto

	id	+	*	()	\$	E
0	s3			s2			1
1		s4	s5			acc	
2	s3			s2			6
3		r4	r4		r4	r4	
4	s3			s2			7
5	s3			s2			8
6		s4	s5		s9		
7		r1	s5		r1	r1	
8		r2	r2		r2	r2	
9		r3	r3		r3	r3	

Error Recovery in LR Parsing

- An LR parser will detect an error when it consults the parsing action table and finds an error entry. All empty entries in the action table are error entries.
- Errors are never detected by consulting the goto table.
- An LR parser will announce error as soon as there is no valid continuation for the scanned portion of the input.
- A canonical LR parser (LR(1) parser) will never make even a single reduction before announcing an error.
- The SLR and LALR parsers may make several reductions before announcing an error.
- But, all LR parsers (LR(1), LALR and SLR parsers) will never shift an erroneous input symbol onto the stack.

Panic Mode Error Recovery

- Scan down the stack until a state s with a goto on a particular nonterminal A is found. (Get rid of everything from the stack before this state s).
- Discard zero or more input symbols until a symbol **a** is found that can legitimately follow A.
 - The symbol a is simply in FOLLOW(A), but this may not work for all situations.
- The parser stacks the nonterminal **A** and the state **goto[s,A]**, and it resumes normal parsing.
- This nonterminal A is normally a basic programming block (there can be more than one choice for A).
 - stmt, expr, block, ...

Phrase-Level Error Recovery

- Each empty entry in the action table is marked with a specific error routine.
- An error routine reflects the error that the user most likely will make in that case.
- An error routine inserts the symbols into the stack or the input (or it deletes the symbols from the stack and the input, or it can do both insertion and deletion).
 - missing operand
 - unbalanced right parenthesis

SLR Tables with Error Actions Action Goto

	id	+	*	()	\$	E
0	s3	e 1	e 1	s2	e2	e 1	1
1	e3	s4	s5	e3	e2	acc	
2	s3	e 1	e 1	s2	e2	e 1	6
3	e 1	r4	r4	e3	r4	r4	
4	s3	e 1	e 1	s2	e2	e 1	7
5	s3	e 1	e 1	s2	e 1	e 1	8
6	e3	s4	s5	e3	s9	e4	
7	e3	r1	s5	e3	r1	r1	
8	e3	r2	r2	e3	r2	r2	
9	e3	r3	r3	e3	r3	r3	

Error Messages

- e1: Expected beginning of expression or subexpression (id or '(')
 - Fix: Shift id into stack and goto state 3 making believe we saw an id
 - If do this, message should be "expected operand"
- e2: Unbalanced right parenthesis
 - Fix: Ignore the ')'
- e3: Found start of subexpression when expecting continuation or end of current subexpression
 - Fix: ??
- e4: Found end of expression when expecting continuation (operator) or end of subexpression (')')
 - Fix: ??